

# Supplemental Material

## I. GRAVITATIONAL REDSHIFT

With  $n = e^\psi$  and  $\Phi = -\frac{c^2}{2}\psi$ , the frequency of a cavity mode scales as

$$\frac{\Delta\nu}{\nu} = -\Delta\psi = -\frac{\Delta\Phi}{c^2}. \quad (1)$$

This reproduces the standard gravitational redshift relation of GR.

## II. GRAVITATIONAL LIGHT DEFLECTION

In the weak field,  $\psi(r) = 2GM/(c^2r)$  and  $n(r) \simeq 1 + \psi(r)$ . For a light ray with impact parameter  $b$  and coordinate  $z$  along the path,  $r = \sqrt{b^2 + z^2}$ . The deflection angle  $\alpha$  follows from Fermat's principle:

$$\alpha \simeq \int_{-\infty}^{\infty} \partial_b n(r) dz \quad (2)$$

$$= \frac{2GM}{c^2} \int_{-\infty}^{\infty} \partial_b \left( \frac{1}{\sqrt{b^2 + z^2}} \right) dz \quad (3)$$

$$= \frac{2GM}{c^2} \left( -b \int_{-\infty}^{\infty} \frac{dz}{(b^2 + z^2)^{3/2}} \right) \quad (4)$$

$$= \frac{4GM}{c^2 b}. \quad (5)$$

This reproduces the full Einstein value, including the factor of two that Einstein's 1911 calculation missed. (*Historical note: Einstein's original 1911 prediction gave only half this value.*)

## III. SHAPIRO TIME DELAY (RADAR ECHO DELAY)

Photon travel time is

$$T = \frac{1}{c} \int n(r) ds \simeq \frac{1}{c} \int \left[ 1 + \frac{2GM}{c^2 r} \right] ds. \quad (6)$$

Relative to flat space, the one-way excess is

$$\Delta t = \frac{2GM}{c^3} \int \frac{ds}{r}. \quad (7)$$

For endpoints at  $r_1, r_2$  with impact parameter  $b$ , this gives

$$\Delta t = \frac{2GM}{c^3} \ln \left( \frac{r_1 + r_2 + L}{r_1 + r_2 - L} \right), \quad (8)$$

with  $L = \sqrt{r_1^2 + r_2^2 - 2r_1 r_2 \cos \theta}$ . The two-way radar delay doubles this to the GR value  $4GM/c^3$ .

## IV. PERIHELION PRECESSION

In isotropic gauge the effective metric to  $\mathcal{O}(\Phi/c^2)$  is

$$ds^2 = - \left( 1 + \frac{2\Phi}{c^2} \right) c^2 dt^2 + \left( 1 - \frac{2\gamma\Phi}{c^2} \right) d\mathbf{x}^2. \quad (9)$$

Here  $\gamma$  is the standard PPN parameter that quantifies spatial curvature per unit Newtonian potential. Its value is fixed by the light-deflection result (5), hence  $\gamma = 1$ . Minimal coupling of matter to this metric yields the Newtonian limit with 1PN corrections corresponding to  $\beta = 1$ . The perihelion shift per orbit in the PPN formalism is

$$\Delta\varpi = \frac{6\pi GM}{c^2 a(1-e^2)} \cdot \frac{2-\beta+2\gamma}{3}, \quad (10)$$

which reduces to the GR value  $\Delta\varpi = 6\pi GM/[c^2 a(1-e^2)]$  when  $\beta = \gamma = 1$ .

## V. COMPARISON TABLE

TABLE I. Weak-field predictions. All classical tests coincide with GR in the weak-field limit; the cavity–atom ratio provides the decisive discriminator.

Observable	GR	DFD
Gravitational redshift	$-\Delta\Phi/c^2$	$-\Delta\Phi/c^2$
Light deflection	$4GM/(c^2b)$	$4GM/(c^2b)$
Shapiro delay (two-way)	$4GM/c^3$	$4GM/c^3$
Perihelion precession	$6\pi GM/[c^2a(1 - e^2)]$	$6\pi GM/[c^2a(1 - e^2)]$
Cavity–atom slope	0	$2\Delta\Phi/c^2$